Mathematics: MCM 109 Final Exam: 1 - 8 - 2011Duration Time: 1 Hour



Academic Year: 2010 – 2011

Semester: Summer

Examiner: Dr. Mohamed Eid

Marks

3

4

5

3

6

3

4

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4

6

6

## **Answer 3 Questions Only**

[1](a) Find y` where: (i) 
$$y = 2x^3 + 4^x$$
 (ii)  $y = \cos x + \log x$  (iii)  $y = x^3 \sin x$ 

(ii) 
$$y = \cos x + \log x$$
 (iii)  $y = x^3 \sin x$ 

(b) Find the integrals: (i) 
$$\int (x^2 + 3^x + 8) dx$$

$$(ii) \int [x^2 + 3]^2 dx$$

(c) Find the eigenvalues and eigenvectors of the matrix 
$$A = \begin{bmatrix} 0 & 1 \\ 4 & 0 \end{bmatrix}$$

[2](a)Determine maximum and minimum values of the function: 
$$f(x) = x^3 - 9$$

(b) Find the integrals: (i) 
$$\int (\frac{1}{x} + \frac{1}{x^2}) dx$$
 (ii)  $\int (\sin x + \frac{2x}{x^2 + 3}) dx$  (ii)  $\int_{0}^{2} (3x^2 + 1) dx$ 

$$(ii)\int (\sin x + \frac{2x}{x^2 + 3})dx$$

(ii) 
$$\int_{0}^{2} (3x^{2} + 1) dx$$

[3](a) Find maximum and minimum values of the function: 
$$f(x) = 2x^2 - 8x + 1$$

(b)If 
$$A = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 3 & -1 \end{bmatrix}$$
,  $B = \begin{bmatrix} 1 & 3 & 2 \\ 1 & 0 & -2 \end{bmatrix}$ . Find, if possible,  $A + B$ ,  $A \cdot B$ ,  $B^t \cdot A$ 

(c)Discuss the consistence of the following linear system (it has one solution, no solution or infinite solutions):

$$2x + 3y - z = 1$$
,  $x - y = 2$ ,  $3x + 2y - z = 4$ 

[4](a)Find the integrals: (i) 
$$\int x \cdot \cos x \, dx$$

(ii) 
$$\int \frac{x+3}{x^2 - 3x + 2} dx$$

(b) If a medicine is available in 3 dosage forms:

First type of concentration: 1 mg /tablet

Second type of concentration: 2 mg /tablet

Third type of concentration: 3 mg /tablet

If the pharmacist wanted to prepare 8 tablets of concentration 2.5 mg/tablet by mixing whole tablets of each type. Find all possible solutions.

Good luck

Dr. Mohamed Eid

Academic Year: 2010 – 2011

Semester: Summer 10 - 7 - 2011Date:

Time: 50 Minutes



Mathematics: MCM 109

Mid-Term Exam

Examiner: Dr. Mohamed Eid

**Answer all questions** 

## [1] Find y` where:

(a) 
$$y = 2x^3 + 4^x$$

(b) 
$$y = \sin x \cdot \log x$$

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 (c)  $y = 8 + \ln(x^3 + x)$  (d)  $y = x^{-3} + x^3$ 

(d) 
$$y = x^{-3} + x^3$$

## [2] Find the integrals:

(a) 
$$\int (x^4 + 3^x) dx$$

(b) 
$$\int (\frac{1}{x} + \cos x) dx$$

(b) 
$$\int (\frac{1}{x} + \cos x) dx$$
 (c)  $\int_{1}^{2} (x^2 + \frac{1}{x^3}) dx$  (d)  $\int x \sin x dx$ 

[3] Find the maximum and minimum values of the function:  $f(x) = 3 + 6x - x^2$ 

[4] A medicine in the blood decreases according to equation  $y_0 - y = 6t$ .

If the initial quantity  $y_0 = 120$  units. Find, time by hours:

- (i) The time at which 40 % of medicine exists in the blood.
- (ii) The time at which 60 % of medicine exists in the blood.
- (iii) The time at which there is no medicine in the blood.

Good luck

Dr. Mohamed Eid

Quiz I 3-7-2011(1) Find f'(x) where: (a)  $f(x) = x^3 + \log x$  (b)  $f(x) = 3^x + 2\cos x$  (c)  $f(x) = x^4 \tan x$ 

(2)Find y` where:

(a)  $y = \frac{\sin x}{x^2}$ 

(b)  $y = 4^x + \frac{1}{x^4}$  (c)  $y = (3+\sin x)^2$ 

(3) Find the maximum and minimum values of the functions:

(a) 
$$f(x) = x^2 - 4x + 2$$
 (b)  $f(x) = x^3 - 3x^2$ 

(b) 
$$f(x) = x^3 - 3x^2$$

$$(c) f(x) = x^3 + 2$$

[1] If  $A = \begin{bmatrix} 1 & 2 \\ 3 & 1 \\ 1 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 2 & 1 & 3 \\ 1 & 0 & 2 \end{bmatrix}$ . Find, if possible, A + B,  $A^t + B$ , A.B, |B.A|

- [2] Write the following linear system and discuss its consistence (it has one solution or no solution or infinite solutions): x + y + z = 6, x - y + 2z = 2,2x + 2y + 2z = 6
- [3] Find the eigenvalues and eigenvectors of the matrix  $A = \begin{bmatrix} 3 & 1 \\ 0 & 1 \end{bmatrix}$